

Soluzione del telaio secondo il Metodo delle Forze (MdF)

à Dati Numerici

```
Clear@EqD;
```

Ü Dati Generali

```

L1 = 400;
L2 = 600;
H = 300;
q = 50;

F = q H
EIt = 288480 30 50^3 ê 12
EIp = 288480 30 30^3 ê 12
KP = N@2050000 Pi 3^2 ê 4 ê Sqrt@L1^2 + H^2DD
Omega = N@ArcTan@H ê L1DD

15000

90150000000

19472400000

28981.2

0.643501

```

Ü Asta AD

AlphaAD = H ê H3 EIpL

AlphaDA = H ê H3 EIpL

BetaAD = H ê H6 EIpL

BetaDA = BetaAD

GammaAD = 0

GammaDA = 0

1
|||||
194724000

1
|||||
194724000

1
|||||
389448000

1
|||||
389448000

0

0

Ü Asta BE

AlphaBE = H ê H3 EIpL

AlphaEB = H ê H3 EIpL

BetaBE = H ê H6 EIpL

BetaEB = BetaBE

GammaBE = 0

GammaEB = 0

1
|||||
194724000

1
|||||
194724000

1
|||||
389448000

1
|||||
389448000

0

0

Ü Asta CG

$$\mathbf{AlphaCG} = \mathbf{H} \hat{\mathbf{e}}_3 \mathbf{EIpL}$$

$$\mathbf{AlphaGC} = \mathbf{H} \hat{\mathbf{e}}_3 \mathbf{EIpL}$$

$$\mathbf{BetaCG} = \mathbf{H} \hat{\mathbf{e}}_6 \mathbf{EIpL}$$

$$\mathbf{BetaGC} = \mathbf{BetaCG}$$

$$\mathbf{GammaCG} = 0$$

$$\mathbf{GammaGC} = 0$$

$$\frac{1}{194724000}$$

$$\frac{1}{194724000}$$

$$\frac{1}{389448000}$$

$$\frac{1}{389448000}$$

$$0$$

$$0$$

Ü Asta DE

$$\mathbf{AlphaDE} = \mathbf{L1} \hat{\mathbf{e}}_3 \mathbf{EI tL}$$

$$\mathbf{AlphaED} = \mathbf{L1} \hat{\mathbf{e}}_3 \mathbf{EI tL}$$

$$\mathbf{BetaDE} = \mathbf{L1} \hat{\mathbf{e}}_6 \mathbf{EI tL}$$

$$\mathbf{BetaED} = \mathbf{BetaDE}$$

$$\mathbf{GammaDE} = q \mathbf{L1}^3 \hat{\mathbf{e}}_{24} \mathbf{EI t}$$

$$\mathbf{GammaED} = -q \mathbf{L1}^3 \hat{\mathbf{e}}_{24} \mathbf{EI t}$$

$$\frac{1}{676125000}$$

$$\frac{1}{676125000}$$

$$\frac{1}{1352250000}$$

$$\frac{1}{1352250000}$$

$$\frac{8}{5409}$$

$$-\frac{8}{5409}$$

Ü Asta EG

```
AlphaEG = L2 ê H3 EItL
AlphaGE = L2 ê H3 EItL
BetaEG = L2 ê H6 EItL
BetaGE = BetaEG
GammaEG = q L2 ^ 3 ê 24 ê EIt
GammaGE = -q L2 ^ 3 ê 24 ê EIt
```

```
1
|||||
450750000
```

```
1
|||||
450750000
```

```
1
|||||
901500000
```

```
1
|||||
901500000
```

```
3
|||||
601
```

```
- 3
- |||||
- 601
```

à Incognite

```
Incognite = {MAD, MCG, MDA, MED, MEG, MGC, MDE, MEB, MGE, Delta};
```

à Equazioni

```
Eq = Table[0, {i, 1, 10}];
```

Ü Equazioni di Congruenza alla rotazione Nodale

```
Eq[[1, DD]] = FiAD;
Eq[[2, DD]] = FiCG;
Eq[[3, DD]] = FiDA - FiDE;
Eq[[4, DD]] = FiED - FiEB;
Eq[[5, DD]] = FiEG - FiEB;
Eq[[6, DD]] = FiGC - FiGE;
```

Ü Equazioni di Equilibrio alla rotazione Nodale

```
Eq[[7, DD]] = MDE + MDA;
Eq[[8, DD]] = MED + MEB + MEG;
Eq[[9, DD]] = MGE + MGC;
```

Ü Equazioni di Equilibrio Globale alla traslazione

$$Eq_{10DD} = -HMDA + MADL \hat{e}_H + MEB \hat{e}_H + HMCG + MGCL \hat{e}_H + F - XE \cos \Omega DL;$$

Ü Definizione delle rotazioni in funzione dei momenti

$$\begin{aligned} FiAD &= \alpha_{AD} MAD - \beta_{AD} MDA + \Delta \hat{e}_H; \\ FiDA &= \alpha_{DA} MDA - \beta_{DA} MAD + \Delta \hat{e}_H; \\ FiDE &= \alpha_{DE} MDE - \beta_{DE} MED + \gamma_{DE}; \\ FiED &= \alpha_{ED} MED - \beta_{ED} MDE + \gamma_{ED}; \\ FiEG &= \alpha_{EG} MEG - \beta_{EG} MGE + \gamma_{EG}; \\ FiGE &= \alpha_{GE} MGE - \beta_{GE} MEG + \gamma_{GE}; \\ FiEB &= \alpha_{EB} MEB + \Delta \hat{e}_H; \\ FiGC &= \alpha_{GC} MGC - \beta_{GC} MCG + \Delta \hat{e}_H; \\ FiCG &= \alpha_{CG} MCG - \beta_{CG} MGC + \Delta \hat{e}_H; \end{aligned}$$

Ü Relazione tra Spostamento e Forza del Pendolo

$$XE = KP \Delta \cos \Omega D;$$

à Soluzione del sistema

$$Sol = NSolve[Eq \sim 0, IncogniteD] \hat{=} Flatten$$

$$\begin{aligned} 8MAD &-402381., MCG &-680239., MDA &-307052., MED &1.6211 \times 10^6, MEG &-1.5069 \times 10^6, \\ MGC &-862768., MDE &307052., MEB &-114194., MGE &862768., Delta &0.383396 < \end{aligned}$$